Paper / Subject Code: 51401 / Applied Mathematics-III - 8 MAY 20

S.E - IT - CBCS

Total Marks: 80

Hours: 3 hrs

Note : 1) Question no. 1 is compulsory.

2) Attempt any three questions out of five questions

Q-1

a) If any 11 numbers between 1 and 20 are chosen show that at least two of them will be (05)multiplies of each other.

b) A function $f: R - \left\{\frac{7}{3}\right\} \to R - \left\{\frac{4}{3}\right\}$ is defined by $f(x) = \frac{4x-5}{3x-7}$, Prove that f is bijective (05)

and find the rule for f^{-1} .

c) Find
$$L\left[\frac{d}{dt}\left(\frac{1-\cos 2t}{t}\right)\right]$$
 (05)
d) Prove that there does not exist an analytic function whose imaginary part is
 $3x^2 + \sin x + y^2 + 5y + 4$. (05)

Q-2

a) Find
$$L^{-1}\left[\frac{s}{\left(s^2+3^2\right)\left(s^2+5^2\right)}\right]$$
 using convolution Theorem. (06)

(06)b) What is the chance of throwing ten with four dice? c) In a certain examination there are multiple choice questions. There are four possible answers to each questions and one of them is correct. An intelligent student can solve 90% questions correctly by reasoning and for the remaining 10% questions he gives answer by guessing. A week student can solve 20% question correctly by reasoning and for the remaining 80% questions he gives answer by guessing. An intelligent student gets the correct (08)answer. What is the probability that he was guessing.

Q-3

a) A can hit a target 2 times in 5 shots, B 3 times in 4 shots, C 2 times in 3 shots. They fire a (06)voliey. What is the probability that at least 2 shots hit the target?

- (06)tan-1 b) Find L
- c) If R is the relation on the set of integers such that aRb if and only if 2a+3b is divisible by 5. (08)Find the equivalence classes.

Evaluate
$$\int_{t=0}^{\infty} e^{-3t} \left(\frac{\cos(7t) - \cos(11t)}{t} \right) dt$$
(06)

$$\text{(06)} \text{ Find } L^{-1}\left[\frac{s^2+2s+3}{\left(s^2+2s+10\right)\left(s^2+2s+17\right)}\right]$$

c) Find the bilinear Transformation which maps the points 2, i, -2 on to the points 1, i, -1. (08)Also find image of |z| = 1 of z-plane to w-plane.

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Q-5

a) A family consisting of an old man, 6 adults and 4 children is to be seated in a row for dinner. The children wish to occupy two seats at each end and the old man refuse to have a child on either side of him. In how many ways can the seating arrangement be made for the dinner? (06)

b) Find the analytic function f(z) = u + iv in terms of z if $u - v = (x - y)(x^2 + 4xy + y^2)$.

c) Solve
$$\frac{d^3y}{dt^3} - 2\frac{d^2y}{dt^2} + 5\frac{dy}{dt} = 0$$
 with $y(0) = 0$, $y'(0) = 0$, $y''(0) = 1$.

Q-6

- a) Prove that $(A-B) \cup (B-A) = (A \cup B) (A \cap B)$
- b) Draw the Hasse diagram of D_{105} .
- c) Find Laplace Transformation of the following i) $te^{3t}erf(5\sqrt{t})$,

ii)
$$\sin tH(t) + (\cos t - \sin t)H(t - \pi$$

(08)

(06)

(06) (06)

(08)

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