## **OP CODE: 24396** IT/SEM OT/CBCS/AM-TO 2018 Marks: 80 (3 Hours) Note: 1. Question no. 1 is compulsory. 2. Attempt any three questions out of remaining five questions. [5] Q.1.[a] Determine the constants a, b, c, d so that the function $f(z) = x^2 + axy + by^2 + i(cx^2 + dxy + y^2)$ is analytic. [b] Let $A = \{1, 2, 3, 4\}, B = \{1, 2, 3, 4\}$ and "aRb if and only if a is not [5] equal to b". Find R and its digraph. [c] For the sets A, B, C given that $A \cap B = A \cap C$ and $\overline{A} \cap B = \overline{A} \cap C$ . Is it necessary that B = C? Justify. 15 [d] Find Laplace transform of f(t) = t for 0 < t < 1= 0 for 1 < t < 2, f(t+2) = f(t).Q.2.[a] 75 Children went to an amusement park where they can ride on [6] the merry-go-round, roller coaster and ferris wheel. It is known that 20 of them have taken all 3 rides, and 55 of them have taken at least two of the 3 rides. Each ride costs 0.50 Rs and the total receipt of the amusement park was 70 Rs. Determine the number of children who did not try any of the rides. [6] [b] Evaluate. $\int_{0}^{\infty} t e^{-3t} J_{0}(4t) dt = \frac{3}{125} \text{ if } L\{J_{0}(t)\} = \frac{1}{\sqrt{s^{2} + 1}}.$ [4] [c] (i) Functions f, g and h are defined as follows : $f: R \rightarrow R$ , $g: R \rightarrow R$ , $h: R \rightarrow R$ , f(x) = x + 4, g(x) = x - 4h(x) = 4x for $x \in R$ , where R is the set of real numbers.

Compute  $f \circ g; g \circ f; f \circ g \circ h; h \circ h$ .

(ii) Show that using Venn diagram  $P \cap (Q-R) = (P \cap Q) - (P \cap R)$ . [4]

Q.3.[a] If f(z) and [f(z)] are both analytic then show that f(z) is constant. [6]

[b] Let R be a binary relation on the set of positive integers such that [6]

 $R = \{(a,b) / a-b \text{ is an odd positive integer }\}$ . Is R reflexive?

Symmetric ? Antisymmetric ? Transitive ? An equivalence relation ?

A partial ordering set?

Page | 1

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343

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